

P31.10 $\Phi_B = (\mu_0 n I) A_{\text{solenoid}}$
 $\varepsilon = -N \frac{d\Phi_B}{dt} = -N \mu_0 n (\pi r_{\text{solenoid}}^2) \frac{dI}{dt}$
 $\varepsilon = -15.0 (4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}) (1.00 \times 10^3 \text{ m}^{-1}) \pi (0.020 \text{ m})^2 (600 \text{ A/s}) \cos(120t)$
 $\varepsilon = -14.2 \cos(120t) \text{ mV}$

P31.12 $|\varepsilon| = \left| \frac{\Delta\Phi_B}{\Delta t} \right| = N \left(\frac{dB}{dt} \right) A = N (0.010 \text{ T} + 0.080 \text{ T/s}) A$
 At $t = 5.00 \text{ s}$, $|\varepsilon| = 30.0 (0.410 \text{ T/s}) [\pi (0.040 \text{ m})^2] = 61.8 \text{ mV}$

P31.22 $F_B = I\ell B$ and $\varepsilon = B\ell v$
 $I = \frac{\varepsilon}{R} = \frac{B\ell v}{R}$ so $B = \frac{IR}{\ell v}$

(a) $F_B = \frac{I^2 \ell R}{\ell v}$ and $I = \sqrt{\frac{F_B v}{R}} = 0.500 \text{ A}$

(b) $I^2 R = 2.00 \text{ W}$

(c) For constant force, $P = \mathbf{F} \cdot \mathbf{v} = (1.00 \text{ N})(2.00 \text{ m/s}) = 2.00 \text{ W}$.

P31.28 (a) $\mathbf{B}_{\text{ext}} = B_{\text{ext}} \hat{\mathbf{i}}$ and B_{ext} decreases; therefore, the induced field is $\mathbf{B}_0 = B_0 \hat{\mathbf{i}}$ (to the right) and the current in the resistor is directed **to the right**.

(b) $\mathbf{B}_{\text{ext}} = B_{\text{ext}} (-\hat{\mathbf{i}})$ increases; therefore, the induced field $\mathbf{B}_0 = B_0 (+\hat{\mathbf{i}})$ is to the right, and the current in the resistor is directed **to the right**.

(c) $\mathbf{B}_{\text{ext}} = B_{\text{ext}} (-\hat{\mathbf{k}})$ into the paper and B_{ext} decreases; therefore, the induced field is $\mathbf{B}_0 = B_0 (-\hat{\mathbf{k}})$ into the paper, and the current in the resistor is directed **to the right**.

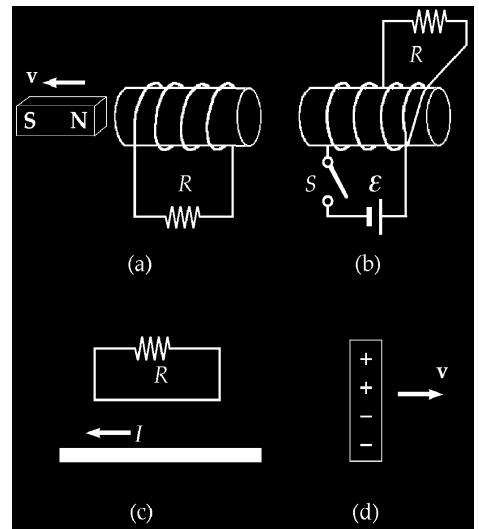


FIG. P31.28

(d) By the magnetic force law, $F_B = q(\mathbf{v} \times \mathbf{B})$. Therefore, a positive charge will move to the top of the bar if \mathbf{B} is **into the paper**.

P31.59 (a) At time t , the flux through the loop is

$$\Phi_B = BA \cos \theta = (a + bt)(\pi r^2) \cos 0^\circ = \pi(a + bt)r^2.$$

At $t = 0$, $\Phi_B = \boxed{\pi ar^2}$.

(b)
$$\varepsilon = -\frac{d\Phi_B}{dt} = -\pi r^2 \frac{d(a + bt)}{dt} = \boxed{-\pi br^2}$$

(c)
$$I = \frac{\varepsilon}{R} = \boxed{-\frac{\pi br^2}{R}}$$

(d)
$$P = \varepsilon I = \left(-\frac{\pi br^2}{R}\right)(-\pi br^2) = \boxed{\frac{\pi^2 b^2 r^4}{R}}$$

P32.8
$$|\varepsilon| = L \frac{dI}{dt} = (90.0 \times 10^{-3}) \frac{d}{dt}(t^2 - 6t) \text{ V}$$

(a) At $t = 1.00 \text{ s}$, $\varepsilon = \boxed{360 \text{ mV}}$

(b) At $t = 4.00 \text{ s}$, $\varepsilon = \boxed{180 \text{ mV}}$

(c) $\varepsilon = (90.0 \times 10^{-3})(2t - 6) = 0$
 when $\boxed{t = 3.00 \text{ s}}$.

P32.18
$$I = \frac{\varepsilon}{R}(1 - e^{-t/\tau}) = \frac{120}{9.00}(1 - e^{-1.80/7.00}) = 3.02 \text{ A}$$

$$\Delta V_R = IR = (3.02)(9.00) = 27.2 \text{ V}$$

$$\Delta V_L = \varepsilon - \Delta V_R = 120 - 27.2 = \boxed{92.8 \text{ V}}$$

P32.46 At different times, $(U_C)_{\max} = (U_L)_{\max}$ so $\left[\frac{1}{2}C(\Delta V)^2\right]_{\max} = \left(\frac{1}{2}LI^2\right)_{\max}$

$$I_{\max} = \sqrt{\frac{C}{L}(\Delta V)_{\max}^2} = \sqrt{\frac{1.00 \times 10^{-6} \text{ F}}{10.0 \times 10^{-3} \text{ H}}}(40.0 \text{ V}) = \boxed{0.400 \text{ A}}$$

P32.32 (a)
$$U = \frac{1}{2}LI^2 = \frac{1}{2}L\left(\frac{\varepsilon}{2R}\right)^2 = \frac{L\varepsilon^2}{8R^2} = \frac{(0.800)(500)^2}{8(30.0)^2} = \boxed{27.8 \text{ J}}$$

(b)
$$I = \left(\frac{\varepsilon}{R}\right)\left[1 - e^{-(R/L)t}\right] \quad \text{so} \quad \frac{\varepsilon}{2R} = \left(\frac{\varepsilon}{R}\right)\left[1 - e^{-(R/L)t}\right] \rightarrow e^{-(R/L)t} = \frac{1}{2}$$

$$\frac{R}{L}t = \ln 2 \quad \text{so} \quad t = \frac{L}{R} \ln 2 = \frac{0.800}{30.0} \ln 2 = \boxed{18.5 \text{ ms}}$$

P32.51 (a) $f = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{(0.0820\text{ H})(17.0 \times 10^{-6}\text{ F})}} = \boxed{135\text{ Hz}}$

(b) $Q = Q_{\max} \cos \omega t = (180\ \mu\text{C}) \cos(847 \times 0.00100) = \boxed{119\ \mu\text{C}}$

(c) $I = \frac{dQ}{dt} = -\omega Q_{\max} \sin \omega t = -(847)(180) \sin(0.847) = \boxed{-114\text{ mA}}$

